nAME \& EID: Solutions

M 427K Quiz 5
October 3, 2012

- Show all work.
- No books, notes, calculators, or other electronic devices.

This problem is about the second order linear nonhomogeneous ordinary differential equation

$$
\begin{equation*}
y^{\prime \prime}+4 y=t^{2}+3 e^{t} \tag{1}
\end{equation*}
$$

1. (10 points) Use the method of undetermined coefficients to find a particular solution to this nonhomogeneous equation. (Just one solution is enough.)

$$
\begin{aligned}
& \text { Try } y=A t^{2}+B t+C+D e^{t} \\
& y^{\prime}=2 A t+B+D e^{t} \\
& y^{\prime \prime}=2 A+D e^{t} \\
& y^{\prime}+4 y=2 A+D e^{t}+4 A t^{2}+4 B t+4 C+4 D e^{t} \\
& =\left(4 A t^{2}+(4 B) t+(2 A+4 C)+5 D e^{t}=t^{2}+3 e^{t}\right. \\
& \text { so } 4 A=1 \Rightarrow A=1 / 4 \\
& 4 B=0 \Rightarrow B=0 \Rightarrow(-2 A)=-\frac{1}{8} \\
& 2 A+4 C=0 \Rightarrow C=\frac{1}{4}=0 \Rightarrow D=3 / 5 \\
& 5 D=3 \Rightarrow D=\frac{1}{4} \Rightarrow t^{2}-\frac{1}{8}+\frac{3}{5} e^{t}
\end{aligned}
$$

